

Information Systems Analysis

# **Temporal Logic and Timed Automata**

(8)

System model verification in NuSMV

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*version 2.6*

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# System modelling

- Indirect modelling
  - Direct modelling
- FAIRNESS constraints
  - Nondeterminism

# System modelling

## Indirect modelling

```
MODULE main

VAR    a : boolean;
       b : 0..4;

ASSIGN    init(a) := TRUE;
           next(a) := !a;
           init(b) := {0,2,4};
           next(b) := case
               next(a) : {0,2,4};
               !next(a) : {1,3};
           esac;

CTLSPEC AG(a -> b in {0,2,4})

INVARSPEC (!a -> b in {1,3})
```

## Direct modelling

```
MODULE main

VAR    a : boolean;
       b : 0..4;

INIT    a = TRUE &
           b in {0,2,4};
TRANS next(a) = !a;
TRANS next(b) in case
           next(a) : {0,2,4};
           !next(a) : {1,3};
       esac;

CTLSPEC AG(a -> b in {0,2,4})

INVARSPEC (!a -> b in {1,3})
```



# System modelling

## Indirect modelling

- Behaviour of an automaton is defined by specifying initial and next values of state variables.
- Example:

```
ASSIGN  init(a) := TRUE;  
        next(a) := !a;  
        init(b) := {0,2,4};  
        next(b) := case  
            next(a)  : {0,2,4};  
            !next(a) : {1,3};  
        esac;
```

- Operator `init` defines the initial value of a variable.
- Operator `next` defines the value of a variable in the next state.

# System modelling

## Indirect modelling

- If the initial value of a variable is not given, it will get any value from its range of values.  
(There exists at least 1 initial state.)
- If the next value of a variable is not given, it will get any value from its range of values.  
(There exists at least 1 next state for every state.)

## Remark

- Every model defined indirectly can be defined directly.
- Not every model defined directly can be defined indirectly.

# System modelling

## Direct modelling

- Behaviour of an automaton is defined by logic expressions.
- Logic expressions express:
  - initial states,
  - reachable states,
  - transitions between states.
- Results of lack of expressions or of their mutual contradiction:
  - an empty set of initial states,
  - unreachable states,
  - lack of reachable states.

# System modelling

## Direct modelling

- Specification of initial values of variables:

```
INIT logic_expression
```

- The expression given after `INIT` describes initial values of variables.
- Example of specification of values of variables `a` and `b`:

```
INIT  a = TRUE &  
      b in {0,2,4}
```

- If the initial value of a variable is not given, it will get any value from its range of values.
- If an untrue expression is given, then there are no initial states (model verification may be incorrect).
- Using the operator `next` is not allowed.

# System modelling

## Direct modelling

- Specification of reachable states by state invariants:

`INVAR logic_expression`

- The expression given after `INVAR` describes the values of variables, that characterise every state.
- Example of specification of values of variables `a` and `b`:

`INVAR a=TRUE | a=FALSE`

`INVAR !a -> b in {1,3}`

- If an untrue expression is given, then there are no reachable states (model verification may be incorrect).
- Invariant definitions are not mandatory.
- Using the operator `next` is not allowed.

# System modelling

## Direct modelling

- Specification of allowed transitions between states:

```
TRANS logic_expression
```

- The expression given after TRANS describes allowed values of variables in the next state.
- Example of specification of next values of variables a and b:

```
TRANS next(a) = !a;  
TRANS next(b) in case  
    next(a) : {0,2,4};  
    !next(a) : {1,3};  
esac;
```

- If an untrue expression is given, then there may be no next state (model verification may be incorrect).

# System modelling

## Direct modelling

- INVAR or INIT combined with TRANS?

- 1<sup>st</sup> way – invariantly  $a = 1$ :

INVAR  $a=1$

- 2<sup>nd</sup> way – in the initial and every following state  $a = 1$ :

INIT  $a=1$

TRANS  $\text{next}(a)=1$

- The effect seems to be the same, but the 1<sup>st</sup> way is more effective.
    - In this situation it is recommended to use an invariant.

# System modelling

## FAIRNESS constraints

- Constraint `JUSTICE expression`
  - Alternatively: `FAIRNESS expression`
  - Model verification consists of these paths only, where the *expression* is true infinitely many times, e.g.:

```
VAR    a : boolean;  
JUSTICE !a
```

- It corresponds to the formula  $AG(AF(\neg(a)))$ .
- Using the operator `next` in the *expression* is not allowed.



# System modelling

## FAIRNESS constraints

- Constraint `COMPASSION (expression1, expression2)`
  - Model verification consists of these paths only, where:
    - if the *expression1* is true infinitely many times,
    - then the *expression2* is also true infinitely many times on the same paths, e.g.:

```
VAR    a : boolean;  
        b : boolean;  
COMPASSION (!a, !b)
```

- It corresponds to the formula  $AG(AG(AF(\neg(a))) \Rightarrow AG(AF(\neg(b))))$ .
- Using the operator `next` in the *expressions* is not allowed.
- NuSMV does not fully support the `COMPASSION` yet.

# System modelling

## Nondeterminism

- Definition of a variable requires to give a set of its values, e.g.:

```
VAR
  a  : 0..10;
  b  : {s1, s2, s3};
```

- If no instruction assigns any value to a variable, then the variable gets a random value of the range of its values.
- If an instruction assigns a subset of a variable's set of values to the variable, then the variable gets a random value of this subset, e.g.:

```
b := {s1, s3}
```

# Mistakes in system modelling

- Different definitions of a variable
- Recursive definition of a variable
- Mutual dependency of variables
- Contradictions in expressions INIT, INVARI and TRANS

# Mistakes in system modelling

## Different definitions of a variable

- Every variable should have one definition only, that defines its value for a given state:
  - wrong: `init(a) := TRUE;`  
`init(a) := FALSE;`
  - wrong: `b := a;`  
`b := a+1;`
  - wrong: `init(c) := a;`  
`c := b;`
  - good: `init(a) := {TRUE, FALSE};`

# Mistakes in system modelling

## Recursive definition of a variable

- Value of a variable cannot depend on its value from the same state:
  - wrong: `a := a+1;`
  - wrong: `next(a) := next(a)+1;`
- But it may depend on its value from the next state:
  - good: `next(a) := a+1;`

# Mistakes in system modelling

## Mutual dependency of variables

- Values of variables in the same state cannot be mutually dependent:
  - wrong:  $a := b+1;$   
 $b := a-1;$
  - wrong:  $\text{next}(a) := \text{next}(b);$   
 $\text{next}(b) := \text{next}(a);$
- But values of variables in different states may be mutually dependent:
  - good:  $\text{next}(a) := b;$   
 $\text{next}(b) := a;$
  - good:  $\text{next}(a) := \text{next}(b);$   
 $\text{next}(b) := a;$

# Mistakes in system modelling

## Contradictions in expressions INIT, INVARIANT and TRANS

- If an untrue expression `INIT` is given, then there are no initial states.
- If an untrue expression `INVARIANT` is given, then there are no reachable states.
- If an untrue expression `TRANS` is given, then there may not be a next state.
- These mistakes are reported by NuSMV.
- These mistakes may lead to an incorrect model verification.

# System verification

- Possibilities
  - Property kinds to verify
- Counting a minimal and maximal path of states



# System verification

## Possibilities

- Verification is automatic.
- Specification of a system is given by temporal logic formulas.
- Available logics: LTL, CTL, LTL<sup>-</sup>, RTCTL (with upper and lower bounds for temporal operators) and PSL.
- All well-formed formulas are allowed.
- Every formulas is verified independently of the others.
- Verification of a formula returns *true* or *false*.
- The *false* result is returned with a counterexample (a path of states), if it can be generated.
- Length of minimal and maximal path between two determined states can be counted.

# System verification

## Property kinds to verify

- Properties described in LTL logic (dealing with linear time):

`LTLSPEC LTL_formula`

- Properties described in CTL logic (dealing with branching time):

`CTLSPEC CTL_formula`

- Properties described in logics LTL<sup>-</sup>, PSL, RTCTL.

- Invariants (dealing with every state of the model):

`INVARSPEC logic_expression`

# System verification

## Counting a minimal and maximal path of states

- Expression `COMPUTE` counts length of a path (number of states) between two specified states.
- Specification of a state is a logic expression expressing values of selected state variables in this state.

- Counting the minimal path:

```
COMPUTE MIN[state1, state2]
```

- Counting the maximal path:

```
COMPUTE MAX[state1, state2]
```

- The result is a number of states or INFINITY.

# Examples

- Departure of a plane (clock and time of events)
- Function with a for loop (analysis of a program's code)

# Examples

## Departure of a plane (clock and time of events)

- **Description of the situation**

- A runway intersects a taxiway.
- An aircraft begins moving before the intersection, accelerating.
- The aircraft, accelerating, reaches the  $V1$  velocity (in 6..8 seconds), and then takes off (in 1..3 seconds).
- The take-off of the aircraft may happen before, on or after the intersection.
- An intruder may appear on the intersection at any moment.
- The intruder, when appears on the intersection, does not disappear from it.
- If the aircraft accelerates before or on the intersection, where the intruder appears, it decelerate, if its velocity  $< V1$ .
- Decelerating aircraft stops (in 3..4 seconds) before, on, or after the intersection.
- If the aircraft and the intruder are on the intersection, a collision may happen.
- Final states: the aircraft takes off, the aircraft stands, there is a collision.

# Examples

## Departure of a plane (clock and time of events)

```
MODULE main
```

```
VAR
```

```
--location of the aircraft
```

```
--in relation to the intersection
```

```
location : {before, on, after};
```

```
--kind of a movement of the aircraft
```

```
movement: {accelerating, decelerating, standing, taking_off};
```

```
--clock for time of the movement (reset to zero at the moment  
--of the beginning of a new movement kind)
```

```
t : 0..9;
```

```
--intruder on the intersection
```

```
intruder : boolean;
```

```
--collision with the intruder
```

```
collision : boolean;
```

```
--aircraft's velocity  $\geq$  v1 (deceleration is forbidden)
```

```
v1 : boolean;
```

# Examples

## Departure of a plane (clock and time of events)

--INITIAL STATE

**INIT**

```
--the aircraft is before the intersection
location = before &
--the aircraft is accelerating
movement = accelerating &
--the time of acceleration begins
t = 0 &
--there is no intruder on the intersection
intruder = FALSE &
--there is no collision
collision = FALSE &
--the aircraft's velocity < v1
v1 = FALSE
```

# Examples

## Departure of a plane (clock and time of events)

--BEHAVIOUR OF THE CLOCK t

**TRANS next(t) in case**

--resetting the clock when taking-off begins

**movement = accelerating & next(movement) = taking\_off : 0;**

--resetting the clock when decelerating begins

**movement = accelerating & next(movement) = decelerating : 0;**

--resetting the clock when standing begins

**movement = decelerating & next(movement) = standing : 0;**

--in other case, with any automaton state change,

--one second passes

**TRUE : (t + 1) mod 10; esac;**



# Examples

## Departure of a plane (clock and time of events)

```
--BEHAVIOUR OF THE INTRUDER
```

```
TRANS next(intruder) in case
```

```
--the intruder may appear at any moment
```

```
!intruder : {FALSE,TRUE};
```

```
--the intruder cannot disappear from the intersection,
```

```
--if it already is there
```

```
TRUE : intruder; esac;
```

# Examples

## Departure of a plane (clock and time of events)

--BEHAVIOUR OF THE v1 VELOCITY

**TRANS next(v1) in case**

--the v1 cannot be reached in the time  $t < 6$

**!v1 & movement = accelerating & next(t)<6 : FALSE;**

--the v1 may be reached in the time  $t < 8$

**!v1 & movement = accelerating & next(t)<8 : {TRUE,FALSE};**

--the v1 is reached at most in the time  $t = 8$

**!v1 & movement = accelerating & next(t)=8 : TRUE;**

--once reached, the v1 velocity does not get smaller

**TRUE : v1; esac;**

# Examples

## Departure of a plane (clock and time of events)

```
--BEHAVIOUR OF THE COLLISION
```

```
--the collision is impossible, if there is no intruder  
--or the aircraft is before the intersection
```

```
INVAR !intruder | location = before -> !collision;
```

```
TRANS next(collision) in case
```

```
  --if there is the collision, it will not pass away
```

```
  collision : TRUE;
```

```
  --if there is no collision, it is possible then,
```

```
  --if the intruder and the aircraft are on the intersection
```

```
  intruder & location = on : {FALSE, TRUE};
```

```
  --other states do not affect the collision
```

```
  TRUE : collision; esac;
```

# Examples

## Departure of a plane (clock and time of events)

--BEHAVIOUR OF THE LOCATION OF THE AIRCRAFT

**TRANS next(location) in case**

--the standing or taking-off aircraft does not change

--its location (final state)

**movement = standing | movement = taking\_off : location;**

--the aircraft being before the intersection may enter it

**location = before : {before, on};**

--the aircraft being on the intersection may leave it

**location = on : {on, after};**

--the aircraft being after the intersection does not change

--its location

**location = after: after; esac;**

# Examples

# Departure of a plane (clock and time of events)

--BEHAVIOUR OF THE MOVEMENT OF THE AIRCRAFT (1)

**TRANS** next (movement) in case

```
--the aircraft accelerating with the velocity >= v1
```

```
--cannot take off if there is the collision
```

-- (no change of movement kind)

```
movement = accelerating & v1 & collision : accelerating;
```

```
--the aircraft accelerating with the velocity >= v1
```

--cannot take off in time  $t < 1$

```
movement = accelerating & v1 & next(t)<1 : accelerating;
```

```
--the aircraft accelerating with the velocity >= v1
```

--may take off in time  $t < 3$  (if there is no collision)

```
movement = accelerating & v1 & next(t)<3 :  
                                {accelerating, taking off};
```

```
--the aircraft accelerating with the velocity  $\geq v_1$  takes off
```

--at last in the time  $t = 3$  (if there is no collision)

```
movement = accelerating & v1 & next(t)=3 : taking off;
```

# Examples

## Departure of a plane (clock and time of events)

```
--BEHAVIOUR OF THE MOVEMENT OF THE AIRCRAFT (2)
```

```
-- ...
```

```
--the aircraft accelerating with the velocity < v1
```

```
--still accelerates, if there is no intruder
```

```
movement = accelerating & !v1 & !intruder : accelerating;
```

```
--the aircraft accelerating with the velocity < v1
```

```
--decelerates, if there is the intruder on the intersection
```

```
movement = accelerating & !v1 & intruder : decelerating;
```

# Examples

## Departure of a plane (clock and time of events)

```
--BEHAVIOUR OF THE MOVEMENT OF THE AIRCRAFT (3)
```

```
-- ...
```

```
--the decelerating aircraft cannot stop in the time  $t < 3$ 
```

```
movement = decelerating & next(t) < 3 : decelerating;
```

```
--the decelerating aircraft may stop in the time  $t < 4$ 
```

```
movement = decelerating & next(t) < 4 :
```

```
{decelerating, standing};
```

```
--the decelerating aircraft will stop at last in the time  $t=4$ 
```

```
movement = decelerating & next(t) = 4 : standing;
```

```
--the standing or taking off aircraft does not change
```

```
--its kind of movement
```

```
movement = standing | movement = taking_off : movement;
```

```
--other states do not affect the movement
```

```
TRUE : movement; esac;
```

# Examples

## Departure of a plane (clock and time of events)

- Verification of behaviour of the clock:

--Incrementation of the clock with every state change (mod 10)

```
CTLSPEC AG(t=0 -> AX(t=1))
```

```
CTLSPEC AG(t=9 -> AX(t=0))
```

```
COMPUTE MIN[t=0,t=1] --should be 1
```

```
COMPUTE MAX[t=0,t=1] --should be 1
```

--Change of a kind of movement of the aircraft resets the clock

--(e.g. change from decelerating to standing)

```
CTLSPEC AG(movement=decelerating & AX(movement=standing)  
                                -> AX(t=0))
```

```
CTLSPEC AG(movement=decelerating & AX(movement=standing) & t!=0  
                                -> AX(t=0))
```



# Examples

## Departure of a plane (clock and time of events)

- Verification of behaviour of the velocity V1:

```
--Accelerating aircraft reaches the v1 velocity  
--in 6..8 seconds
```

```
CTLSPEC EF(!v1 & movement=accelerating -> EX v1)  
CTLSPEC AG(!v1 & movement=accelerating & AX t=8 -> AX v1)  
CTLSPEC AG(!v1 & movement=accelerating & AX t<6 -> AX !v1)  
CTLSPEC AG(!v1 & movement=accelerating & AX t>=6 & AX t<8  
                                         -> EX !v1)    --correct  
CTLSPEC AG(!v1 & movement=accelerating & AX t>=6 & AX t<8  
                                         -> AX !v1)    --incorrect
```

# Examples

## Function with a for loop (analysis of a program's code)

- The function calculates the sum of numbers from 0 to x:

```
int sum(int x){  
    int s = 0; //sum of numbers  
    for(int i = 0; i <= x; i++)  
        s = s + i;  
    return s;}  

```

- The goal – analyse the for loop, e.g.:
  - find the maximal number of the loop execution,
  - check reachability of s=21 for x=6.

# Examples

## Function with a for loop (analysis of a program's code)

- Labels of executed operations:

```
int sum(int x){  
    int s = 0; //sum of numbers      e0 (this can be omitted)  
    for(int i = 0; i <= x; i++)      e1  
        s = s + i;                  e2  
    return s;}                      e3
```

- Model of the operations:

```
MODULE main  
FROZENVAR x : 0..6;    --constant x of random value of 0 to 6  
VAR e : {e1, e2, e3}; --labels of operations  
    s : 0..21;          --sum of numbers  
    i : 0..7;           --iterator of the loop  
    c : 0..6;           --counter of loop executions  
    a : 1..3;           --flag of reachability of deadlock
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                    e2  
  return s;}                      e3
```

- Model of the operations:

### ASSIGN

--navigation of operations:

**init(e) := e1;**                   --beginning in e1

**next(e) := case**

**e = e1 & i <= x : e2;**   --transition to e2 from e1 if i<=x  
    --(to perform the first operation from the for block)

**e = e1 & i > x : e3;**   --transition to e3 from e1 if i>x  
    --(not to perform operations from the for block)

**e = e2 : e1;**           --return to e1 from e2  
    --(the last operation from the for block is done)

**e = e3 : e3; esac;**   --no entry from e3 (the end of program)

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s;}                      e3
```

- Model of the operations:

### ASSIGN

--variability of s:

```
init(s) := 0;           --initially s=0  
next(s) := case  
  s + i > 21 : s;       --no change of s  
                  --(not to exceed its range)  
  next(e) = e2 : s + i; --i is added to s (in operation e2)  
  TRUE : s; esac;      --no change of s  
                  --(in other cases)
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s;}                      e3
```

- Model of the operations:

### ASSIGN

--variability of i:

```
init(i) := 0;           --initially i=0  
next(i) := case  
  i + 1 > 7 : i;        --no change of i  
                        --(not to exceed its range)  
  next(e) = e1 : i + 1;  --incrementation of i  
                        --(in operation e1, i.e. after e2)  
  TRUE : i; esac;       --no change of i  
                        --(in other cases)
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s;}                      e3
```

- Model of the operations:

### ASSIGN

--variability of c:

```
init(c) := 0;           --initially c=0  
next(c) := case  
  c + 1 > 6 : c;        --no change of c  
                        --(not to exceed its range)  
  next(e) = e2 : c + 1; --incrementation of c  
                        --(in operation e2, i.e. for block)  
TRUE : c; esac;        --no change of c  
                        --(in other cases)
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
    int s = 0; //sum of numbers  
    for(int i = 0; i <= x; i++)  
        s = s + i;  
    return s;}  
e1  
e2  
e3
```

- Model of the operations:

### ASSIGN

--variability of a:

**init(a) := 1;** --initially a=1 (there will be a next state)

**next(a) := case**

**a = 1 & e = next(e) & s = next(s) & i = next(i) & c = next(c) : 2;**  
--a is set to 2

--(if there is no change of state for the 1<sup>st</sup> time)

**a = 2 : 3;** --a is set to 3

--(so 2 be in one state only)

**TRUE : a; esac;** --no change of a

--(in other cases)



# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x) {  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s; }                     e3
```

- Verification of the model:
  - Does the flag *a* work correctly?

```
CTLSPEC AF (a=2 & AX (AG (a=3) ) )      true
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x) {  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s; }                     e3
```

- Code analysis:

- What is the maximal length of the path of states to the final state?

COMPUTE MAX[a=1, a=2] **16**

- What is the maximal number of the *for* loop execution?
  - generate a maximal length path,
  - check the final value of the *c* counter on the path.

CTLSPEC !EBF 16..16 (a=2) **false** **c = 6**

```
-> State: 5.12 <-  
  e = e2  
  s = 15  
  c = 6  
-> State: 5.13 <-  
  e = e1  
  i = 6  
-> State: 5.14 <-  
  e = e2  
  s = 21  
-> State: 5.15 <-  
  e = e1  
  i = 7  
-> State: 5.16 <-  
  e = e3  
-> State: 5.17 <-  
  a = 2
```

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x) {  
    int s = 0; //sum of numbers  
    for(int i = 0; i <= x; i++)    e1  
        s = s + i;                e2  
    return s; }                  e3
```

- Code analysis:
  - Can the *for* loop be executed 6 times?

CTLSPEC EF (c=6)            **false**

CTLSPEC !EF (c=6)          **false**

**How is it possible?**

- Is the sum  $s = 21$  reachable?

CTLSPEC EF (s=21)          **false**

CTLSPEC !EF (s=21)        **false**

**How is it possible?**

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x) {  
    int s = 0; //sum of numbers  
    for(int i = 0; i <= x; i++)      e1  
        s = s + i;                  e2  
    return s; }                     e3
```

- Code analysis:
  - If there is more than 1 initial state, then reachability checking for a given state by the formula  $EF(\text{state\_to\_check})$  will return *false*, if this state is not reachable from every initial state, even so if it is reachable from some initial state.
    - solution 1: choose an initial state:  
 $\text{initial\_state} \rightarrow EF(\text{state\_to\_check})$
    - solution 2: check non-reachability of the state:  
 $\neg EF(\text{state\_to\_check})$

# Examples

## Function with a for loop (analysis of a program's code)

```
int sum(int x){  
  int s = 0; //sum of numbers  
  for(int i = 0; i <= x; i++)      e1  
    s = s + i;                     e2  
  return s; }                     e3
```

- Code analysis:

- Is the sum  $s = 21$  reachable?

```
CTLSPEC x=6 -> EF(s=21)      true  
CTLSPEC !EF(s=21)            false
```

- Will the sum  $s = 21$  be reached?

```
CTLSPEC x=6 -> AF(s=21)      true
```

# Interactive work

- Initial operations
- Model verification
- Model simulation
- Restart and end of work
- Executions of a script with operations
- Description of operations performed by NuSMV

# Interactive work

## Initial operations

- Start working with a .smv file in the interactive mode:

```
NuSMV -int file
```

- Read the model of a system:

```
read_model
```

- Create modules and processes:

```
flatten_hierarchy
```

- Show a list of input variables and state variables:  
(optional)

```
show_vars
```

# Interactive work

## Initial operations

- Show variables that are dependent on a given expression:  
(optional)

```
show_dependencies -e expression
```

- Create variables to compile the model into BDD (binary decision diagrams):

```
encode_variables
```

- Write the order of variables to a file:  
(optional)

```
write_order
```

- Compile the model into BDD:

```
build_model
```



# Interactive work

## Initial operations

- Initialise the system ready to be verified:

```
go
```

- Read and compile the model into BDD, verify the model and count a set of reachable states:

```
process_model
```

- Count a set of reachable states:

```
compute_reachable
```

- Show reachable states:  
(optional)

```
print_reachable_states -v
```

# Interactive work

## Model verification

- Show all properties:

```
show_property
```

- Add a property of a given kind to the verification:

```
add_property -kind -p "formula"
```

- Add the property to verification in the context of a given module:

```
add_property -kind -p "formula IN module"
```

Kind: *c* (CTL formula), *l* (LTL formula), *s* (PSL formula), *i* (invariant),  
*q* (counting a path).

# Interactive work

## Model verification

- Verify a CTL formula of a given number:

```
check_ctlspec -n number
```

- Verify a given CTL formula:

```
check_ctlspec -p "formula"
```

- Verify a given CTL formula in the context of a given module:

```
check_ctlspec -p "formula IN module"
```

Similarly for LTL specification: `check_ltlspec`

# Interactive work

## Model verification

- Check possibility of a deadlock of the system:

```
check_fsm
```

- Count length of a path between given states (for a given number of an expression):

```
check_compute -n number
```

- Count length of the minimal path between given states:

```
check_compute -p "MIN[state1,state2]"
```

- Count length of the maximal path between given states in the context of a given module:

```
check_compute -p "MAX[state1,state2] IN module"
```

# Interactive work

## Model verification

- Verify an invariant of a given number:

```
check_invar -n number
```

- Verify a given invariant:

```
check_invar -p "invariant"
```

- Verify a given invariant in the context of a given module:

```
check_invar -p "invariant IN module"
```

# Interactive work

## Model simulation

- Choose randomly an initial state:

```
pick_state -r
```

- Choose an initial state from the list of available states:

```
pick_state -i
```

- Choose an initial state from a restricted list of available states  
– the states that satisfy a given expression:

```
pick_state -i -c "expression"
```

# Interactive work

## Model simulation

- Make a simulation from a chosen state:

```
simulate [-p|-v] [-r|-i] [-k number_of_states]
```

- show changed state variables: `-p`
- show all state variables: `-v`
- randomly choose from available states: `-r`
- manually choose from available states: `-i`
- give length of path of states (e.g. 4): `-k 4`

(The simulation consists of 10–state paths by default.)

- examples:

```
simulate -p -r -k 5  
simulate -v -i
```

# Interactive work

## Model simulation

### Analysis of a chosen path of states:

- Paths of states are created in result of a negative verification of a formula, and in result of a simulation.
- Show generated paths:
  - all: `show_traces -v -a`
  - a chosen one: `show_traces -v path_number`
  - a chosen one with states (from – to):  
`show_traces -v  
path_number.from_state_number:to_state_number`
- Show a number of generated paths:  
`show_traces -t`



# Interactive work

## Model simulation

### Analysis of a chosen path of states:

- Go to a chosen state of a chosen path:

```
goto_state path_number.state_number
```

- Show description of the current state of the current path:

```
print_current_state -v
```

# Interactive work

## Restart and end of work

- Restart of work (reset of adjustments):

`reset`

- End of work (reset of adjustments):

`quit`

# Interactive work

## Executions of a script with operations

- Automatically make a given sequence of operations from a file:

```
NuSMV -source file
```

- If an error occurs, further operations cannot be executed.

## Description of operations performed by NuSMV

- Set verbosity of performed operations:

```
NuSMV -v N -int file
```

(N – level of verbosity: from 0 (nothing) to 4)

# The end

## Literature:

- K.L. McMillan, „The SMV system”, 2001
- A. Cimatti et al. „NuSMV – a new symbolic model checker”
- R. Cavada et al. „NuSMV 2.5 User Manual”, 2010
- R. Cavada et al. „NuSMV 2.5 Tutorial”