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$$\mu(u) = c_1 \varphi_1(u) + c_2 \varphi_2(u) + \dots + c_m \varphi_m(u)$$

$$y_k = \sum_{i=0}^{s-1} \delta_i \mu(u_{k-i}) = \delta_0 [c_1 \varphi_1(u_k) + c_2 \varphi_2(u_k) + \dots + c_m \varphi_m(u_k)] + \delta_1 [c_1 \varphi_1(u_{k-1}) + c_2 \varphi_2(u_{k-1}) + \dots + c_m \varphi_m(u_{k-1})] + \dots + \delta_{s-1} [c_1 \varphi_1(u_{k-(s-1)}) + \dots + c_m \varphi_m(u_{k-(s-1)})] + z_k =$$

$$= \begin{bmatrix} \delta_0 c_1 \\ \vdots \\ \delta_0 c_m \\ \delta_1 c_1 \\ \vdots \\ \delta_1 c_m \\ \vdots \\ \delta_{s-1} c_1 \\ \vdots \\ \delta_{s-1} c_m \end{bmatrix} \begin{bmatrix} \varphi_1(u_k) \\ \vdots \\ \varphi_m(u_k) \\ \varphi_1(u_{k-1}) \\ \vdots \\ \varphi_m(u_{k-1}) \\ \vdots \\ \varphi_1(u_{k-(s-1)}) \\ \vdots \\ \varphi_m(u_{k-(s-1)}) \end{bmatrix} + z_k = \Theta^T \cdot \Phi_k + z_k$$

$k=1, 2, \dots, N$

$$Y_N = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix}$$

$$\Phi_N = \begin{bmatrix} \leftarrow \phi_1^T \rightarrow \\ \leftarrow \phi_2^T \rightarrow \\ \vdots \\ \leftarrow \phi_N^T \rightarrow \end{bmatrix}$$

$$Z_N = \begin{bmatrix} z_1 \\ \vdots \\ z_N \end{bmatrix}$$

$$\hat{\Theta} = (\Phi_N^T \Phi_N)^{-1} \Phi_N^T Y_N \xrightarrow{N \rightarrow \infty} \Theta$$